

Fig. 1.32

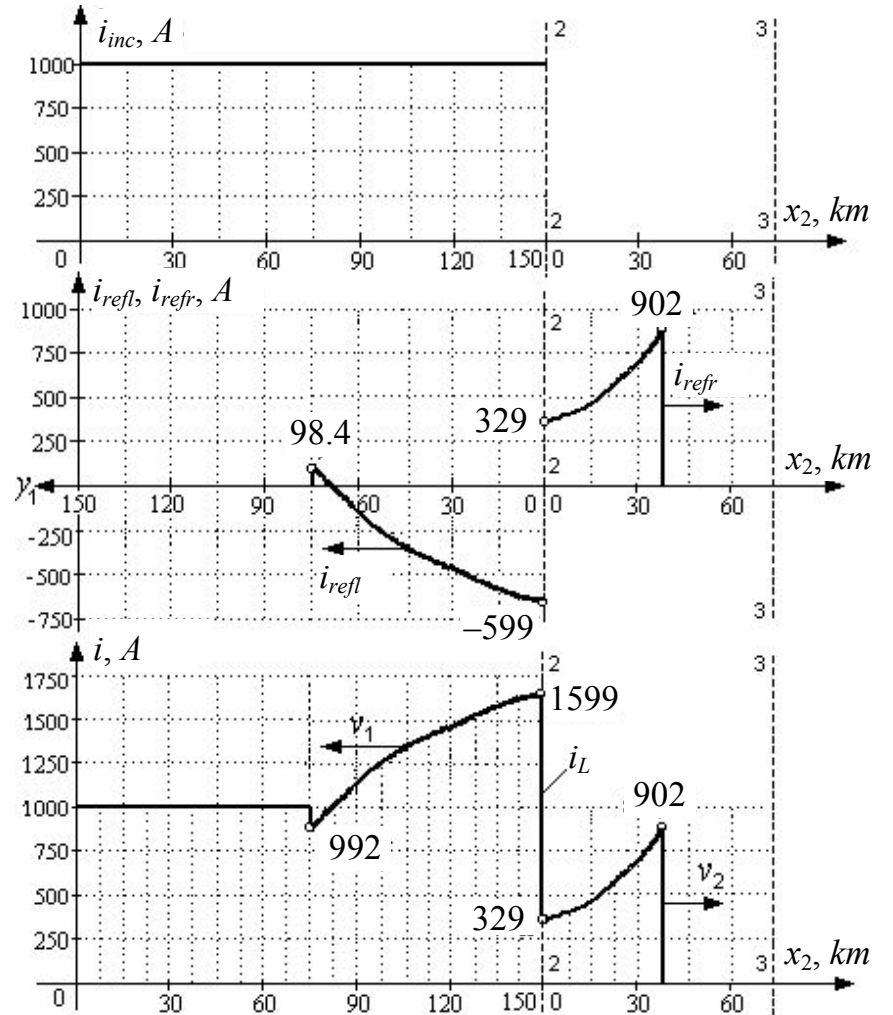
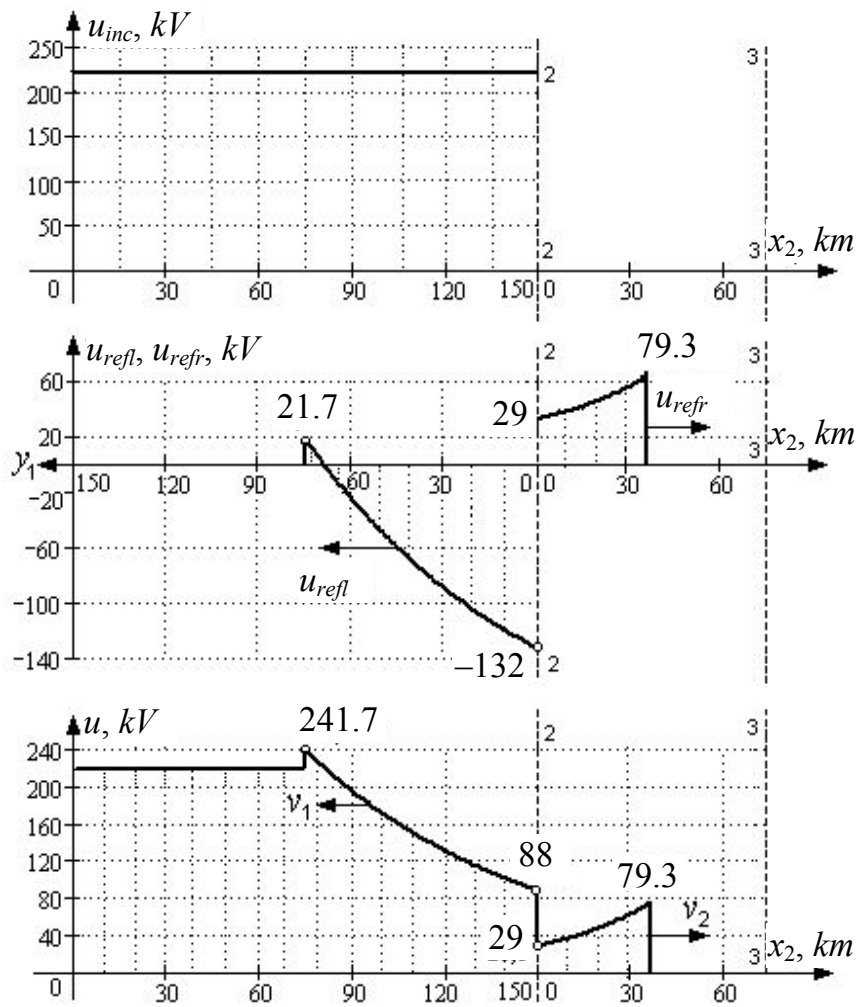
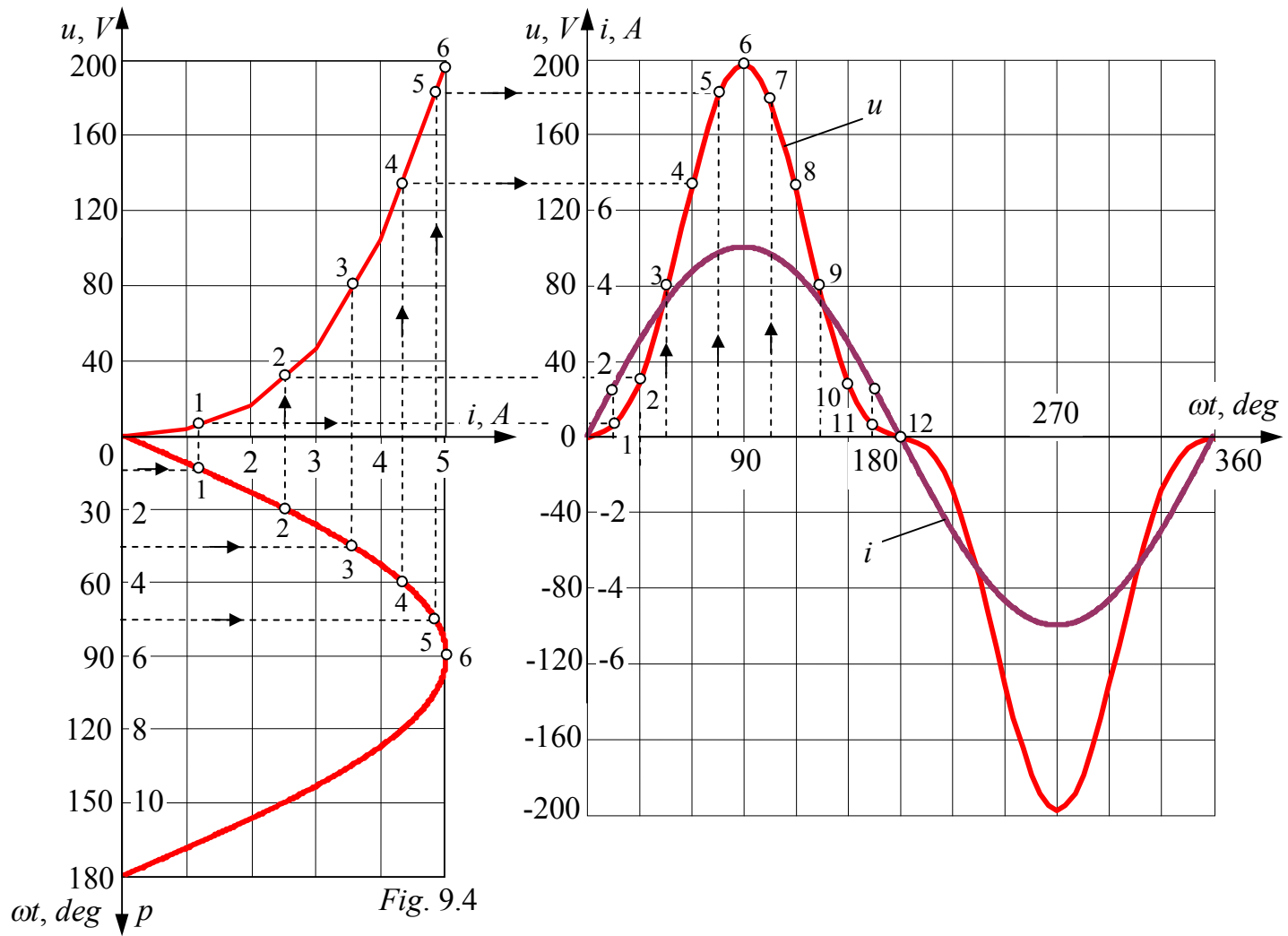


Fig. 8.30



APPENDIX

Operator	Coordinate system		
	Cartesian	Cylindrical	Spherical
Gradient φ , $grad\varphi \equiv \nabla\varphi$	$\frac{\partial\varphi}{\partial x}\bar{i} + \frac{\partial\varphi}{\partial y}\bar{j} + \frac{\partial\varphi}{\partial z}\bar{k}$	$\frac{\partial\varphi}{\partial r}\bar{r}_0 + \frac{1}{r}\frac{\partial\varphi}{\partial\alpha}\bar{\alpha}_0 + \frac{\partial\varphi}{\partial z}\bar{z}_0$	$\frac{\partial\varphi}{\partial R}\bar{R}_0 + \frac{1}{R}\frac{\partial\varphi}{\partial\theta}\bar{\theta}_0 + \frac{1}{R\sin\theta}\frac{\partial\varphi}{\partial\alpha}\bar{\alpha}_0$
Divergency \bar{A} , $div\bar{A} \equiv \nabla \cdot \bar{A}$	$\frac{\partial A_x}{\partial x} + \frac{\partial A_y}{\partial y} + \frac{\partial A_z}{\partial z}$	$\frac{1}{r} \left[\frac{\partial}{\partial r} (rA_r) + \frac{\partial A_\alpha}{\partial\alpha} \right] + \frac{\partial A_z}{\partial z}$	$\frac{1}{R^2} \frac{\partial (R^2 A_R)}{\partial R} + \frac{1}{R\sin\theta} \frac{\partial (A_\theta \sin\theta)}{\partial\theta} + \frac{1}{R\sin\theta} \frac{\partial A_\alpha}{\partial\alpha}$
Rotor \bar{A} , $rot\bar{A} \equiv \nabla \times \bar{A}$	$\begin{vmatrix} \bar{i} & \bar{j} & \bar{k} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ A_x & A_y & A_z \end{vmatrix}$	$\begin{vmatrix} \bar{r}_0/r & \bar{\alpha}_0 & \bar{z}_0/r \\ \frac{\partial}{\partial r} & \frac{\partial}{\partial\alpha} & \frac{\partial}{\partial z} \\ A_r & rA_\alpha & A_z \end{vmatrix}$	$\begin{vmatrix} \bar{R}_0/R^2 \sin\theta & \bar{\theta}_0/R \sin\theta & \bar{\alpha}_0/R \\ \frac{\partial}{\partial R} & \frac{\partial}{\partial\theta} & \frac{\partial}{\partial\alpha} \\ A_R & RA_\theta & R\sin\theta A_\alpha \end{vmatrix}$
Laplacian (nonvector) $\nabla^2\varphi$	$\frac{\partial^2\varphi}{\partial x^2} + \frac{\partial^2\varphi}{\partial y^2} + \frac{\partial^2\varphi}{\partial z^2}$	$\frac{1}{r} \frac{\partial}{\partial r} (r \frac{\partial\varphi}{\partial r}) + \frac{1}{r^2} \frac{\partial^2\varphi}{\partial\alpha^2} + \frac{\partial^2\varphi}{\partial z^2}$	$\frac{1}{R^2} \left[\frac{\partial}{\partial R} (R^2 \frac{\partial\varphi}{\partial R}) + \frac{1}{\sin\theta} \frac{\partial}{\partial\theta} (\sin\theta \frac{\partial\varphi}{\partial\theta}) + \frac{1}{\sin^2\theta} \frac{\partial^2\varphi}{\partial\alpha^2} \right]$